

1 Spatio-Temporal Reconstruction of Missing Forest 2 Microclimate Measurements

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13 14 **Abstract**

15 Scientists and land managers are increasingly monitoring forest microclimate environments to
16 better understand ecosystem processes, such as carbon sequestration and the population
17 dynamics of species. Obtaining reliable time-series measurements of microclimate conditions is
18 often hindered by missing and erroneous values. In this study, we compare spatio-temporal
19 techniques, space-time kriging (probabilistic) and empirical orthogonal functions (deterministic),
20 for reconstructing hourly time series of near-surface air temperature recorded by a dense network
21 of 200 forest understory sensors across a heterogeneous 349 km² region in northern California.
22 The reconstructed data were also aggregated to daily mean, minimum, and maximum in order to
23 understand the sensitivity of model predictions to temporal scale of measurement. Empirical
24 orthogonal functions performed best at both the hourly and daily time scale. We analyzed several
25 scenarios to understand the effects that spatial coverage and patterns of missing data may have

26 on model accuracy: (a) random reduction of the sample size/density by 25%, 50%, and 75%
27 (*spatial coverage*); and (b) random removal of either 50% of the data, or three consecutive
28 months of observations at randomly chosen stations (random and seasonal *temporal missingness*,
29 respectively). Here, space-time kriging was less sensitive to scenarios of spatial coverage, but
30 more sensitive to temporal missingness, with less marked differences between the two
31 approaches when data were aggregated on a daily time scale. This research contextualizes trade-
32 offs between techniques and provides practical guidelines, with free source code, for filling data
33 gaps depending on the spatial density and coverage of measurements.

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35 Keywords (max 6): missing data, spatio-temporal prediction, microclimate sensors, empirical
36 orthogonal functions, near-surface air temperature, California.

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52 **1. Introduction**

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54 The availability of complete long-term, high-resolution datasets of climatic conditions
55 measured near the earth’s surface is crucial for understanding ecological processes affected by
56 environmental heterogeneity (McDonald and Urban, 2004; Meentemeyer, 1978; Turner and
57 Chapin, 2005; Waring and Running, 1998). Fluctuations in these microclimate (Geiger, 1965)
58 conditions may influence processes such as the dynamic evolution of an infectious disease in
59 natural ecosystems (Meentemeyer et al., 2012), species distributions (Gehlhausen et al., 2000),
60 and the structure of landscape patterns of carbon and nutrient cycling (Band et al., 1991). In
61 forest ecosystems, weather conditions have historically been measured either at insufficient
62 spatial densities to capture landscape-level variation in microclimate (Lookingbill and Urban,
63 2003) or at a “representative” site often cleared of vegetation (Bolstad et al., 1998).
64 Technological advancements have led to high resolution data sets becoming more affordable and
65 common, but this has produced a fresh challenge. Even when high-resolution meteorological and
66 hydrologic observational datasets are obtained they are frequently beset with periods of missing
67 data caused by the failure of data loggers (e.g. due to power outages), climatological events (e.g.
68 snow, ice, or precipitation) (Henn et al., 2013), and even cattle interference (personal
69 observation). In other cases, erroneous or unreasonable values are recorded and must be
70 manually removed. Establishing effective and efficient methods for predicting microclimate
71 conditions to fill in these gaps will increase the utility of these datasets for examining thresholds
72 governing ecological dynamics at fine spatial and temporal scales.

73 Accurately filling in the missing data at fine spatial and temporal resolutions provide the
74 necessary detail for modeling organisms that interact, but may respond differently to similar

75 environmental conditions (e.g. a plant pathogen versus its host). A complete data set also allows
76 for examination and testing of environmental thresholds under natural conditions. For example,
77 the number of hours or days at or above (or below) a threshold temperature for disease
78 development may be used to help predict whether a pest or pathogen is likely to occur, such as
79 the models developed for controlling powdery mildew on grapes (Thomas et al., 1994). Seasonal
80 averages of maximum or minimum daily temperatures at specific locations have also been used
81 to assess the sensitivity of *Ixodes pacificus* tick densities (a Lyme disease carrier) in California
82 forests, requiring finely resolved spatial and temporal data (Swei et al., 2011). These detailed
83 data enable empirically based predictions of how pest-pathogen-host interactions may respond to
84 future climate conditions (e.g. Caffarra et al. 2012).

85 Several statistical methods are available for reconstructing time series of missing air
86 temperature data. In general, techniques for estimating missing data are similar to spatial
87 interpolation, extrapolation, and forecasting in that available observations are used to reconstruct
88 missing observations (Henn et al., 2013). Common spatial interpolation techniques include thin-
89 plate splines (Pape et al., 2009), inverse-distance weighting (Daly et al., 2000), radial basis
90 functions (Myers, 1992), and kriging (Cressie, 1993; Garen et al., 1994; Tobin et al., 2011).
91 Temporally correlated processes are typically modeled using autoregressive time series (Raible
92 et al., 1999). The above techniques are concerned either with estimating unknown values for
93 single temporal realizations (spatial domain), or separately for each station regardless of their
94 spatial proximity (temporal domain). Recent advancements in the theory of spatio-temporal
95 processes have extended the above techniques for application to processes correlated in time and
96 space (Cressie and Wikle, 2011).

97 In this paper, we present a framework, with comparison of two statistical techniques, for
98 estimating missing time series data collected across heterogeneous landscapes. We specifically
99 examined (i) probabilistic space-time kriging (Cressie and Wikle, 2011; Heuvelink and Griffith,
100 2010) on residuals from temporally-smoothed data and (ii) deterministic spatio-temporal
101 correlations in the form of empirical orthogonal functions (EOF) (Beckers and Rixen, 2003;
102 Lorenz, 1956). We applied these methods to an unusually dense network of hourly temperature
103 measurements collected in forest understory environments across a spatially heterogeneous
104 landscape. Although temperature measurements are often needed at different temporal scales
105 (e.g. hourly, daily) depending on the analysis, for example, how species and communities
106 respond to climate (Bolstad et al., 1998), little attention has been given to studying how temporal
107 aggregation impacts the performance of methods for reconstructing missing data. A previous
108 study inspected the effect of temporal aggregation on spatial prediction of understory
109 temperature using physiographic and ecological factors over the same area used herein
110 (Vanwalleghem and Meentemeyer, 2009). However, the presence of temporal dependence in the
111 temperature time series was ignored in favor of focusing on single temporal aggregations, e.g.
112 average maximum temperature for the month.

113 In this study, we address several key questions: how does a geostatistical technique
114 (space-time kriging) compare to a deterministic one (EOF) when trying to accurately estimate
115 data gaps in microclimate measurements? How does spatial coverage (i.e. sampling size and
116 density of stations) and temporal completeness (i.e. amount of missing data and gap length)
117 affect the accuracy of model estimates? Do larger temporal aggregations of observations
118 influence model accuracy?

119 Finally, we offer guidelines and free source code for practitioners to fill gaps in
120 understory temperature data, depending on the spatial density of available microclimate stations,
121 duration of the missing data, and scale of analysis.

122 Section 2 describes the study area, the temperature dataset, and the methodologies used to
123 reconstruct the missing data across scenarios of spatial coverage and temporal gaps. Results are
124 presented in section 3. Section 4 presents discussions and conclusions based on the results of the
125 study.

126

127 **2. Materials and Methods**

128

129 The steps required to pre-process the available dataset and all subsequent statistical
130 analyses were implemented in the R environment for statistical computing (R Core Team, 2013),
131 and we provide free source code¹.

132

133 2.1. Study area and data

134

135 During 2003, we established 200 ecological monitoring sites in forested stands across a
136 349-km² heterogeneous area in Sonoma County, California (Fig. 1). Sonoma County experiences
137 a Mediterranean climate, with distinct wet and dry seasons (Barbour and Billings, 2000).
138 Precipitation typically falls as rain from October through April, and a dry season occurs from
139 May through September. The landscape is a mix of public and private property near the cities of
140 Santa Rosa, Petaluma, and Sonoma with varying levels of agricultural and urban development

¹ <https://github.com/f-tonini/Microclimate-Sonoma>

141 (Fig. 1A). The forested areas are characterized by open oak woodlands, denser stands of mixed
142 evergreen trees, and a few locations dominated by Coast redwood or Douglas-fir. Sites were
143 randomly located across the forested landscape, resulting in an elevation gradient of the geo-
144 referenced site centers from 55 m to 800 m (mean = 378 m). Each site was equipped with a
145 microclimate data logger, and has been revisited annually through 2014 to monitor conditions
146 and download the data. Initially, each location had a temperature/relative humidity data logger
147 (model H08-032-08; Onset Computer Corporation, Bourne, MA, USA) installed inside a solar
148 radiation shield (model RS1, Onset Computer Corporation, Bourne, MA, USA) 1-m off the
149 ground (Fig. 1C). These loggers began to fail in 2008, and so they were replaced with new
150 temperature-only data loggers (model UA-001-64, Onset Computer Corporation, Bourne, MA,
151 USA) inside the same solar radiation shields (Fig. 1B). During this ongoing project different
152 personnel have managed data collection, leading to inconsistencies in the setting of the temporal
153 resolution of the loggers across the sites and between years. In the remainder of this paper we
154 address this challenge, as well as methods for handling varying levels of missing data that may
155 often plague datasets collected over many years.

156

157 **Figure 1-caption at the end of file**

158

159 2.2. Data processing

160

161 Several pre-processing steps were necessary in order to prepare the data for the analysis:

162 (1) temperature values from each data logger were pre-screened to check for outliers exceeding
163 plausible maximum and minimum values; (2) The full database was aligned to match a common

164 hourly resolution. Data recorded at intervals shorter than an hour were averaged. This step was
165 required because some data loggers recorded temperature values at different time intervals (e.g.
166 30, 45 minutes). (3) The full database was sliced to begin on May 1st, 2003 and end on April 30th,
167 2014 in order to keep a large number of available stations every year (≥ 100). (4) Time series
168 points in which the rate of change between hours was considered excessive were replaced by a
169 missing-value flag. In this case, a rate of change $>4^{\circ}\text{C h}^{-1}$ was chosen as reasonable threshold
170 based on other studies (Henn et al., 2013). (5) Lastly, temperature time series were visually
171 inspected for each station to spot the presence of erroneous patterns (e.g. if a data logger kept
172 recording data after being removed from the field). If present, these data points were replaced
173 with a missing-value flag.

174 The analyses presented herein were conducted using data from the year 2004, which
175 together with 2005 had the largest number of actively recording stations ($n = 200$). Overall, 10%
176 of the observations were missing for 2004, providing a good trade-off between missing data and
177 number of useable stations for testing the performance of our models. A map showing the
178 percentages of missing values at each station for the year 2004 can be found in Appendix A
179 (online version).

180

181 2.3. Statistical methods

182

183 We incorporated spatio-temporal correlations between observations and estimated missing
184 values in the recorded time series of understory temperature by using (i) local space-time kriging
185 (STK, hereafter) (Cressie and Wikle, 2011; Heuvelink and Griffith, 2010) and (ii) empirical
186 orthogonal functions (EOF, hereafter) (Beckers and Rixen, 2003; Lorenz, 1956). These two
187 statistical approaches were chosen to compare a geostatistical (STK) to a deterministic (EOF)

188 technique, and because of their applicability to different fields of study, such as oceanography
 189 and meteorology (Alkuwari et al., 2013; Beckers and Rixen, 2003; Hengl et al., 2012; Lorenz,
 190 1956; Youzhuan et al., 2008; Yu and Chu, 2010). Deterministic techniques, compared to
 191 geostatistical ones, do not make use of any *a priori* hypothesis based on some probability
 192 distributions and, hence, no statistical test (Cressie, 1993). An outline of the theory, main
 193 assumptions, and modeling settings used in each technique follows.

194

195 2.3.1. Local space-time kriging

196

197 Consider a continuous variable Z , e.g. temperature, varying over a spatial domain S and
 198 a time interval T . Let $z(\mathbf{s}_i, t_i), i = 1, 2, \dots, n$ be a set of n data observed at a finite set of
 199 locations in space and points in time, where \mathbf{s} is a vector of spatial coordinates, $\{\mathbf{s} = (x, y)\}$,
 200 and t represents a series of points in time. In a space-time geostatistical framework, unobserved
 201 values $z(\mathbf{s}_0, t_0)$ are typically predicted at a number of nodes (\mathbf{s}_0, t_0) of a spatio-temporal grid.
 202 Predictions are made by exploiting the spatio-temporal correlation between observed locations
 203 $z(\mathbf{s}_i, t_i)$ using techniques such as kriging (Cressie, 1993). Commonly used kriging models
 204 include space-time ordinary kriging and universal kriging, also known as kriging with an
 205 external drift (Hengl et al., 2012). Kriging requires directly estimating spatio-temporal
 206 covariances or, more commonly, the semivariances between observed values using spatio-
 207 temporal variograms as follows:

$$208 \quad \gamma(h, u) = \frac{1}{2n(h, u)} \sum_{i=1}^{n(h, u)} [z(\mathbf{s}_i, t_i) - z(\mathbf{s}_i + h, t_i + u)]^2,$$

209 where γ measures the average dissimilarity between data separated by a given spatial and
210 temporal lag (h, u) , where h is the Euclidean spatial distance $|\mathbf{h}|$ and u is the time interval.

211 A diverse range of models have been proposed to capture the structure of spatio-temporal
212 autocorrelation, including the product model (Rodriguez-Iturbe and Mejia, 1974), the metric
213 model (Dimitrakopoulos and Luo, 1994), the product-sum model (De Cesare et al., 2001), and
214 the sum-metric model (Heuvelink et al., 2012). The sum-metric model was adopted for this study
215 because it handles the space-time interaction in a flexible way, without imposing symmetry
216 constraints between the spatial and temporal correlation components. The sum-metric variogram
217 structure is defined as:

$$218 \quad \gamma(h, u) = \gamma_S(h) + \gamma_T(u) + \gamma_{ST} \left(\sqrt{h^2 + (\alpha \cdot u)^2} \right), \quad (1)$$

219 where $\gamma(h, u)$ represents the semivariance for h and u units of spatial and temporal distance,
220 respectively. $\gamma_S(h)$ describes the purely spatial components, while $\gamma_T(u)$ describes the purely
221 temporal component. The space-time interaction component is described by $\gamma_{ST}(h, u)$, where
222 the geometric anisotropy between space and time, i.e. the range variation in different dimensions,
223 is handled by the parameter α , which converts units of temporal distances into units of spatial
224 distance (Kilibarda et al., 2014). In local space-time kriging, the spatio-temporal covariance
225 function is evaluated only for the “strongest” neighbors of a prediction point, i.e. only the first n
226 number of observations with the strongest correlation are used, with n assigned by the user.

227 It is necessary to remove large-scale spatial trends and seasonality prior to investigating
228 the spatio-temporal covariance structure of the data because space-time kriging assumes
229 stationarity and spatial isotropy (Kilibarda et al., 2014). For this purpose, a loess (“locally-
230 weighted scatterplot smoothing”) smoothing curve (Cleveland and Devlin, 1988) was applied

231 separately for each station and residuals of each temperature time series were used for local
232 space-time kriging (e.g. Fig. 2).

233

234 **Figure 2-caption at the end of file**

235

236 All spatio-temporal kriging models were implemented using the gstat (Pebesma, 2004),
237 spacetime (Pebesma, 2012), and stats (R Core Team, 2013) R packages.

238

239 2.3.2. Empirical orthogonal functions

240

241 The spatio-temporal correlation structure of a dataset may also be described by a set of
242 orthogonal functions, called empirical orthogonal functions. Let $T_n(t)$ represent the temperature
243 values recorded at N stations as a function of time. Assuming these values are observed at M
244 times, t_1, t_2, \dots, t_M , it is possible to expand $T_n(t)$ as follows:

245
$$T_n(t_i) = \sum_{k=1}^N Y_{kn} Q_k(t_i)$$

246 where Y_{kn} represent the time-independent basis functions, i.e. EOF, and $Q_k(t_i)$ represent time-
247 dependent coefficients or weights. Standard singular value decomposition (SVD) techniques
248 (Klema and Laub, 1980) can be applied to the spatio-temporal dataset matrix to generate a set of
249 EOF, where the first orthogonal components contain the bulk of the variance and explain the
250 dominant patterns of spatio-temporal variation (Beckers and Rixen, 2003). The leading
251 components are most likely to describe large-scale spatio-temporal patterns, while the latter ones
252 might contain a mix of local-scale patterns and instrument noise (Henn et al., 2013). EOF can be
253 considered as a set of optimally defined functions of space with associated temporal weights at

254 each time. However, SVD cannot be used when a dataset matrix contains missing data. To
255 overcome this issue, Beckers and Rixen (2003) developed a parameter-free iterative estimation
256 technique to reconstruct both missing data and the complete EOF. Missing data are first replaced
257 by an unbiased guess, i.e. the overall dataset mean, and then iteratively estimated by using a
258 truncated series of EOF until reaching convergence. A detailed description of the estimation
259 algorithm can be found in Appendix B (online version). EOF have been widely applied in both
260 oceanography and meteorology (Beckers and Rixen, 2003; Lorenz, 1956; Youzhuan et al., 2008;
261 Yu and Chu, 2010), as well as used in statistical downscaling methods in geophysics (Alkuwari
262 et al., 2013). A recent study applied the EOF reconstruction technique to estimate missing values
263 in air temperature datasets (Henn et al., 2013). The truncated EOF algorithm was implemented
264 using a set of R functions (R Core Team, 2013), following the method proposed by Beckers and
265 Rixen (2003).

266

267 2.4. Missing data scenarios

268

269 We developed three scenarios of missing data to assess the influence of spatial coverage
270 and temporal completeness on the efficacy of each statistical technique for filling data gaps in
271 space and time. Specifically, we artificially altered the number of sampling locations (sampling
272 size/density), the number of randomly missing observations, and serial missingness of
273 observations (consecutively missing observations at different times and at different locations).
274 Each scenario is described in further detail in the following sections.

275

276 2.4.1. Sampling size/density scenario

277

278 We examined the case in which the available network of microclimate stations has a
279 lower spatial density. The complete set of available microclimate stations ($n = 200$, 0.57
280 stations/km²) was artificially altered by removing an increasing number of locations.
281 Specifically, we examined reductions in sampling size of 25% ($n = 150$, 0.43 stations/km²), 50%
282 ($n = 100$, 0.29 stations/km²), and 75% ($n = 50$, 0.14 stations/km²). In each case, stations were
283 removed in a randomized fashion (see Fig. 3 A-D). We reconstructed microclimate
284 measurements only within these spatially reduced datasets, without any attempt to spatially
285 interpolate values at locations that were removed from the original dataset.

286

287 **Figure 3-caption at the end of file**

288

289 2.4.2. Gap length and amount of missing values scenario

290

291 We also examined cases where the missing data may not be stations but temporal gaps
292 instead. These temporal gaps may be in the form of either random occurrence (random
293 missingness) or a long section of consecutively missing values (seasonal missingness). To
294 examine these two types of missing data the available spatio-temporal dataset matrix was either
295 artificially altered by randomly removing 50% of the observations (random missingness, Fig.
296 4C), or randomly removing three consecutive months of observations (seasonal missingness, Fig.
297 4B).

298

299

Figure 4-caption at the end of file

300

301 2.5. Performance metrics

302

303 We evaluated each statistical technique in terms of prediction accuracy, ignoring missing
304 values in the dataset during model evaluation. A 10-fold cross validation was carried out, where
305 a single subsample was retained as the validation data for testing the model, while using the
306 remaining portion for model training. The following prediction metrics were quantified in order
307 to compare the original data to model predictions:

308 *Root-mean-square error (RMSE):*

309 The root-mean-square error is defined as follows:

$$310 \text{RMSE} = \sqrt{\frac{1}{m} \sum_{i=1}^m [\hat{T}(\mathbf{s}_i, t_i) - T(\mathbf{s}_i, t_i)]^2},$$

311 where $\hat{T}(\mathbf{s}_i, t_i) - T(\mathbf{s}_i, t_i)$ represents the difference between the predicted and observed
312 temperature at space-time points (\mathbf{s}_i, t_i) and m is the length of the time series of observations for
313 each station. The root-mean-square error was also used in the iterative EOF reconstruction
314 algorithm as a criterion to determine the optimal number of EOF for minimizing the error (see
315 Appendix B, online version, for more details).

316 *Mean absolute error (MAE):*

317 The mean absolute error is a simple arithmetic average of the absolute errors and is defined as
318 follows:

$$319 \text{MAE} = \frac{1}{m} \sum_{i=1}^m |\hat{T}(\mathbf{s}_i, t_i) - T(\mathbf{s}_i, t_i)|$$

320 *Mean-square-error skill score:*

321 A skill score measures the forecast accuracy with respect to the accuracy of a reference forecast.
322 Positive values correspond to a skill, while negative ones correspond to no skill. The mean-
323 square-error skill score (SS_{MSE}) is defined as follows:

$$324 \quad SS_{MSE} = 1 - \frac{MSE}{MSE_{ref}},$$

325 where MSE is defined as the quantity within the square root in the RMSE formula above. SS_{MSE}
326 was calculated by using the observed average as baseline reference (Murphy, 1988).

327 *Correlation coefficient (COR):*

328 Perhaps the simplest overall measure of performance, the correlation coefficient is defined as:

$$329 \quad COR = \frac{Cov(\hat{T}(s_i, t_i), T(s_i, t_i))}{s_{\hat{T}} s_T},$$

330 where $s_{\hat{T}}$ and s_T indicate the standard deviations of predicted and observed temperature values,
331 respectively. The correlation coefficient measures the linear association between forecast and
332 observation. However, it only performs well when data are normally distributed and it is
333 extremely sensitive to large values and outliers (Taylor, 2001).

334 Both the RMSE and MAE disregard the direction of over- or under- prediction. All four
335 metrics were averaged over the total number of available stations to come up with an overall
336 measure of accuracy. However, these can also be calculated and mapped separately for each
337 station to assess where the statistical techniques had higher/lower accuracy (Fig. C.1-C.2,
338 Appendix C, online version). In order to analyze the impact of temporal aggregation on
339 prediction accuracy the original dataset and modeled predictions were aggregated from an hourly
340 to daily resolution (daily mean, maximum, and minimum). Days for which this aggregation
341 process did not remove missing values were ignored in the calculation of both performance
342 metrics.

343

344 3. Results

345

346 3.1. Exploratory Data Analysis

347

348 In order to inspect the degree to which pairs of time series are correlated, we selected a
349 group of microclimate stations in close proximity (Fig. 5A) and looked at the cross-correlation
350 function (CCF) (Berezin et al., 2012).

351

352 **Figure 5-caption at the end of file**

353

354 Similar patterns of cross-correlations (Fig. 5B) suggested the presence of a strong spatial
355 dependence among stations in close proximity. The extended correlation over time can perhaps
356 be explained by the buffering effect that forest canopies have on the hourly temperature
357 measurements. This preliminary analysis was replicated on other groups of stations and revealed
358 approximately the same patterns of spatio-temporal dependency.

359

360 3.2. Local space-time kriging for hourly temperature

361

362 Residuals from loess-smoothed hourly temperature data show a clear spatio-temporal
363 correlation pattern (Fig. 6A), following the main hypothesis of space-time variograms, i.e. the
364 spatial structure becomes weaker as the time differences increase (Fig. 6B). Therefore, spatio-
365 temporal kriging of residuals is applicable.

366

367

Figure 6-caption at the end of file

368

369 The three components of the sum-metric variogram model and their parameters (Table 1)
370 were chosen based on the combination that gave the best accuracy in predicting the observed
371 hourly temperature.

372

373

Table 1-caption at the end of file

374

375 The parameters show that all components are needed to capture the residual spatio-temporal
376 pattern in the loess-smoothed time series of hourly temperature. The range parameters in both the
377 purely spatial and joint space-time components are very large, indicating that the residuals are
378 correlated over distances up to ~240 km. The highest prediction accuracy for the local space-time
379 kriging technique was reached when setting the maximum number of neighbors equal to 10 (i.e.
380 using the 10 strongest correlated). The spatio-temporal anisotropy ($\alpha = 2.96$ m/hour) shows that
381 stations with a temporal lag of 1 day exhibit a similar correlation as stations that are about 70
382 meters ($2.96 * 24$) apart.

383

384 3.3. Empirical orthogonal functions for hourly temperature

385

386 The iterative EOF estimation routine (Appendix B, online version) suggested that the
387 optimal number of orthogonal functions to use with the hourly temperature measurements is
388 equal to nine (Fig. 7). The RMSE starts leveling out after the first six components until reaching
389 a minimum for nine EOF. This number is considered as the optimal number of EOF needed to

390 explain most spatio-temporal variability found in the hourly temperature dataset. The first EOF
391 alone explained 55% of the dataset variance, and the first nine together explained about 70%.

392

393 **Figure 7-caption at the end of file**

394

395 3.4. Comparison of model predictions

396

397 Both STK and EOF predicted hourly temperatures accurately (Fig. 8A-B), with a
398 correlation of about 0.98 between predicted and observed values for each method. A slightly
399 higher heteroscedasticity can be observed for STK (Fig. 8A).

400

401 **Figure 8-caption at the end of file**

402

403 We selected two temporal windows from the hourly time series of a representative microclimate
404 station to show the resulting predictions for both statistical techniques. The reconstructed time
405 series of hourly temperatures shows some differences between the two models (Fig. 9A-B). The
406 extended gap length likely affected model predictions over the missing portion of the time series
407 (Fig. 9A). The reconstructed values show a similar variability between the two methods, with
408 STK predicting lower hourly temperature values compared to EOF. The high prediction accuracy
409 of both techniques is confirmed by looking at the reconstructed values over a portion of available
410 data (Fig. 9B). Although similar in their accuracy, the EOF technique predicted the observed
411 time series better compared to STK.

412

413 **Figure 9-caption at the end of file**

414

415 Performance differences between STK and EOF were more pronounced at the hourly
416 temporal resolution compared to the chosen daily aggregations (mean, max, min), with
417 magnitudes depending on the missing data scenario used (Fig. 10). The model performance
418 measured in terms of MAE, MSE skill score (SS_{MSE}), and COR confirmed a similar trend to that
419 observed for the RMSE (Appendix D, online version). Overall, the EOF technique predicted the
420 observed time series of data more accurately (lower RMSE and MAE, higher COR and SS_{MSE})
421 than STK regardless of the temporal aggregation. The accuracy of both modeling methods
422 converged as the sampling size/density was reduced, indicating that the performance of EOF
423 degrades rapidly as spatial coverage decreases. Conversely, STK was less sensitive to the
424 reduction of sampling density with only slight decreases in model accuracy. At the daily
425 resolution, prediction accuracy was almost identical when 75% of the stations were removed,
426 however, at an hourly resolution EOF provided greater accuracy. EOF was affected by the
427 random and seasonal temporal missingness scenarios to a lesser extent than STK.

428

429 **Figure 10-caption at the end of file**

430

431 **4. Discussion and Conclusions**

432

433 Our focus was to accurately reconstruct incomplete forest microclimate measurements
434 rather than inspecting the relative importance of ecological and physiographic variables on
435 microclimate dynamics (e.g. Vanwallegem and Meentemeyer, 2009).

436

437 Results indicate that a reduction in sampling size/density has a greater effect on EOF
model predictions than temporal missingness. In contrast, STK was more affected by temporal

438 missingness compared to EOF, with seasonal gaps (ss_noise) reducing STK prediction accuracy
439 more than the presence of a larger number of randomly missing data (rnd_noise). The lower
440 performance of the space-time kriging technique in these settings may be explained by a lack of
441 stationarity and spatial isotropy of the spatio-temporal covariance structure (Kilibarda et al.,
442 2014). We speculate that additional temporal gaps contributed to degrading stationarity and
443 spatial isotropy. Stationarity assumptions are likely inaccurate when evaluating the raw (hourly)
444 temperature data, leading to less accurate predictions. We tried to address this issue by using
445 residuals of loess-smoothed time series, separately for each station, and by using a flexible
446 space-time variogram model. In contrast, EOF offers a convenient method for characterizing
447 dominant spatial patterns of variability by exploiting the spatio-temporal covariance structure
448 without making any assumptions on the probabilistic distribution of data. The effect of the
449 number of stations for the automatic EOF reconstruction routine has been demonstrated in a
450 previous study, where the method performed best with more than 16 stations (Henn et al., 2013).
451 Temporal aggregation reduced the error in each modeling technique, as well as the differences in
452 the accuracy between them, with the lowest RMSE values for both EOF and STK observed when
453 modeling the daily mean. The smaller differences between model accuracies at the daily
454 resolution can be explained by fewer missing values left in the dataset after aggregation.

455 Depending on the characteristics of their dataset, Fig. 10 can instruct practitioners on the
456 different trade-offs that need to be considered when choosing a method for filling in missing
457 temperature data recorded by understory microclimate stations. On the basis of the above results,
458 it was clear that the station density, the amount of missing values, and the length of data gaps
459 affected the performance of the chosen statistical methods. Although people have successfully
460 used kriging with as few as seven data points (Jernigan, 1986), successful applications also

461 depend on the extent of the study area over which they are distributed. On the one hand, a
462 general rule of thumb in the literature appears to be around a minimum of 30 stations (ASTM
463 Standard D5922, 2010). On the other hand, although a large amount of data typically improves
464 the predictive power of space-time kriging, it can also pose computational challenges due to the
465 *big n* problem (Banerjee et al., 2004). Whenever the primary goal is to predict temperature data
466 at unobserved locations, space-time kriging represents the most common and immediate solution
467 to spatially interpolate observed data and have an associated measure of prediction uncertainty.
468 The use of space-time kriging requires a fair amount of time to calibrate all the parameters and
469 tune the model (see section 3.2), thus representing a limitation compared to the automatic EOF
470 estimation routine.

471

472 4.1. Guidelines for reconstructing missing forest microclimate measurements

473

474 We herein summarize general “rules-of-thumb” and trade-offs between the two statistical
475 approaches in order to guide method selection:

- 476 • EOF should be preferred over STK for highly correlated hourly observations. The
477 increase of temporal aggregation levels (e.g. daily) resulting in a smaller
478 dependence among observations reduces discrepancies between predictive
479 performance of EOF and STK.
- 480 • Use EOF when dealing with either random or consecutive seasonal patterns of
481 temporal gaps in the observations. Discrepancies between the predictive
482 performance of both modeling approaches decrease when increasing temporal
483 aggregation.

- 484 • Use STK when interpolating values at unobserved locations. Although this
485 methodology has been successfully applied to small numbers of ground stations
486 over small spatial extents, a minimum of 30 stations should be used as a rule-of-
487 thumb. EOF would simply apply the mean value of all the observations to the
488 unobserved locations, thus not capturing physical influences.
- 489 • STK should be preferred over EOF for sparse networks of ground stations (< 50
490 or 0.14 stations/ km²) with few temporal gaps (preferably random) in the
491 available observations.

492 We demonstrated methods to reconstruct hourly time series of microclimate data by
493 exploiting the spatio-temporal correlation between microclimate sensors placed under forest
494 canopy and compared the predictive accuracies of two spatio-temporal statistical techniques, a
495 geostatistical (STK) and a deterministic one (EOF), in reconstructing hourly time series of data.
496 To the best of our knowledge, this is the first study to quantify in a comprehensive way the
497 performance of both methods at a landscape-level based on several missing data scenarios as
498 well as the impact of temporal aggregation. A dense network of 200 microclimate stations
499 allowed us to analyze the impact that sampling size/density, the overall amount of missing data,
500 and the length of data gaps had on model predictions. The framework presented herein could be
501 used to assimilate multiple data sources measured at different temporal resolutions providing an
502 avenue for integrating key aspects of fine-scale spatial heterogeneity into ecosystem studies.

503

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505

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516 Southwest Research Station.

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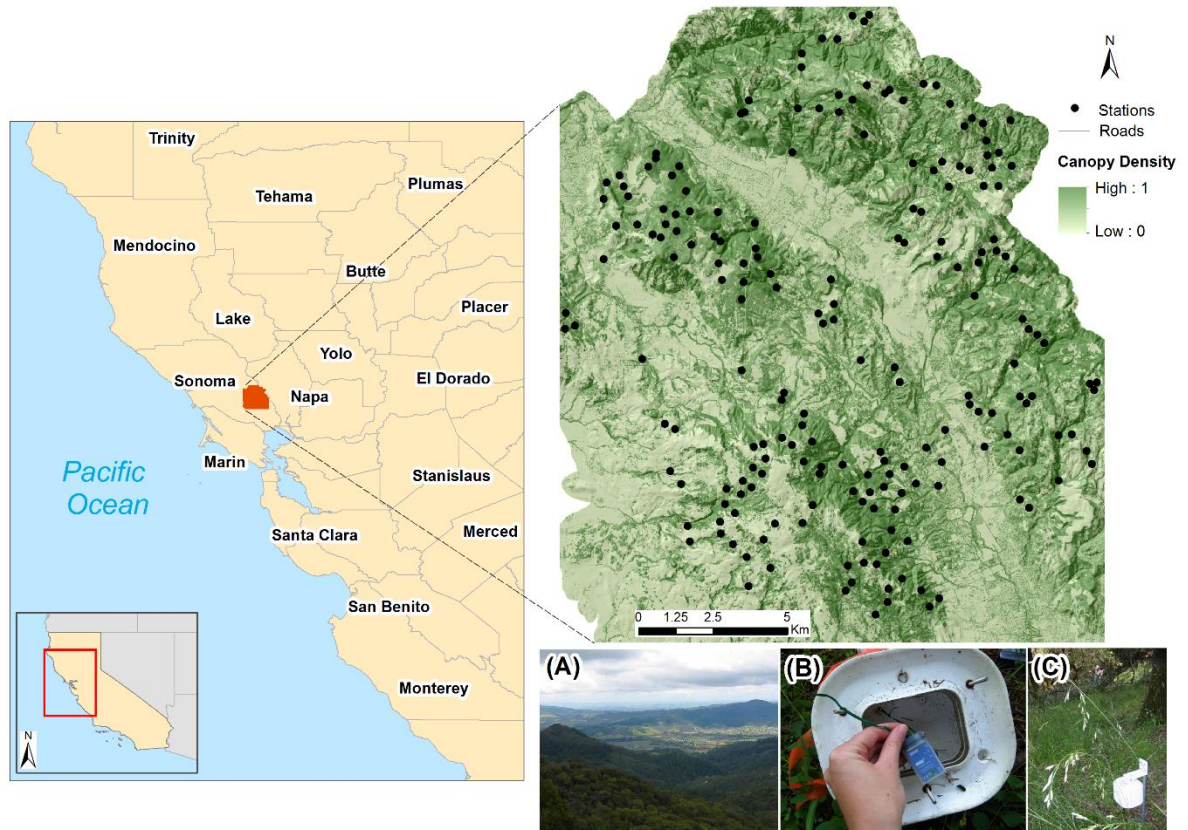
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657 **Figure 1** Overview of the Sonoma study system, California, with indication of canopy
 658 density and microclimate sensor locations. (A) Photo of the landscape characteristic of the
 659 study area. (B) The temperature-only logger installed beginning in 2008, and (C) A solar
 660 radiation shield housing the temperature logger installed in the forest understory (HOBO
 661 H8 Pro, Onset Corp., Bourne, MA, USA). Available in color online.

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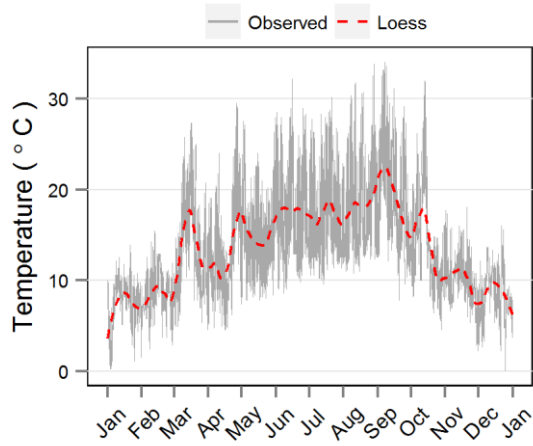
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671 **Figure 2 Hourly temperature (gray solid line) and loess smoother (span = 0.1) of hourly**

672 **temperature (red dashed line) for station ANN01. Available in color online.**

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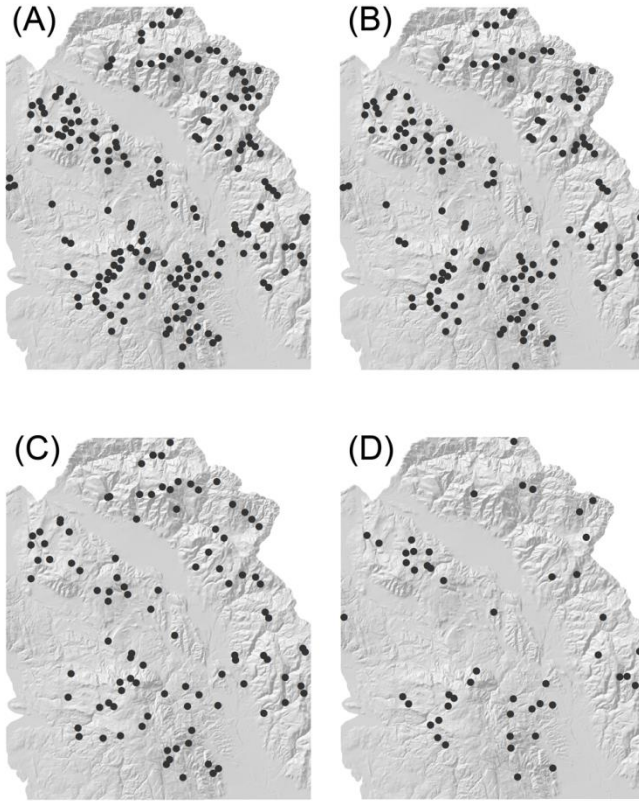
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693 **Figure 3 Sampling size/density reduction scenarios. (A) All locations ($n = 200$, 0.57**
694 **stations/km²). (B) Random removal of 25% of the stations from the original network ($n =$**
695 **150 , 0.43 stations/km²). (C) Random removal of 50% of the stations from the original**
696 **network ($n = 100$, 0.29 stations/km²). (D) Random removal of 75% of the stations from the**
697 **original network ($n = 50$, 0.14 stations/km²).**

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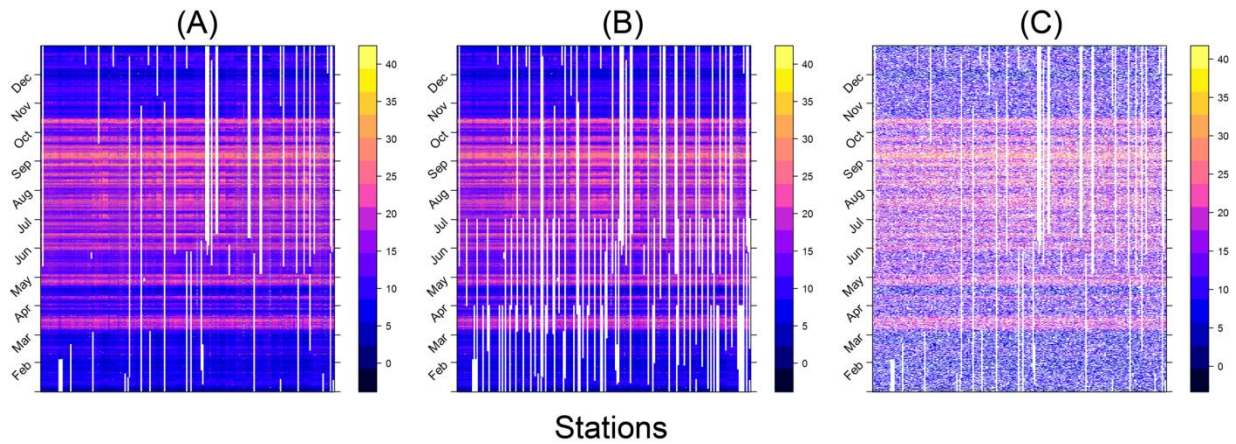
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706 **Figure 4 Data removal scenarios. (A) Original hourly temperature measurements in 2004.**

707 **(B) Randomized removal of consecutive 3-month blocks of hourly temperature**

708 **measurements for randomly selected stations (C) Randomized removal of 50% of hourly**

709 **temperature measurements. Lighter areas correspond to higher temperature values.**

710 **Completely white sections are missing data. Available in colors online.**

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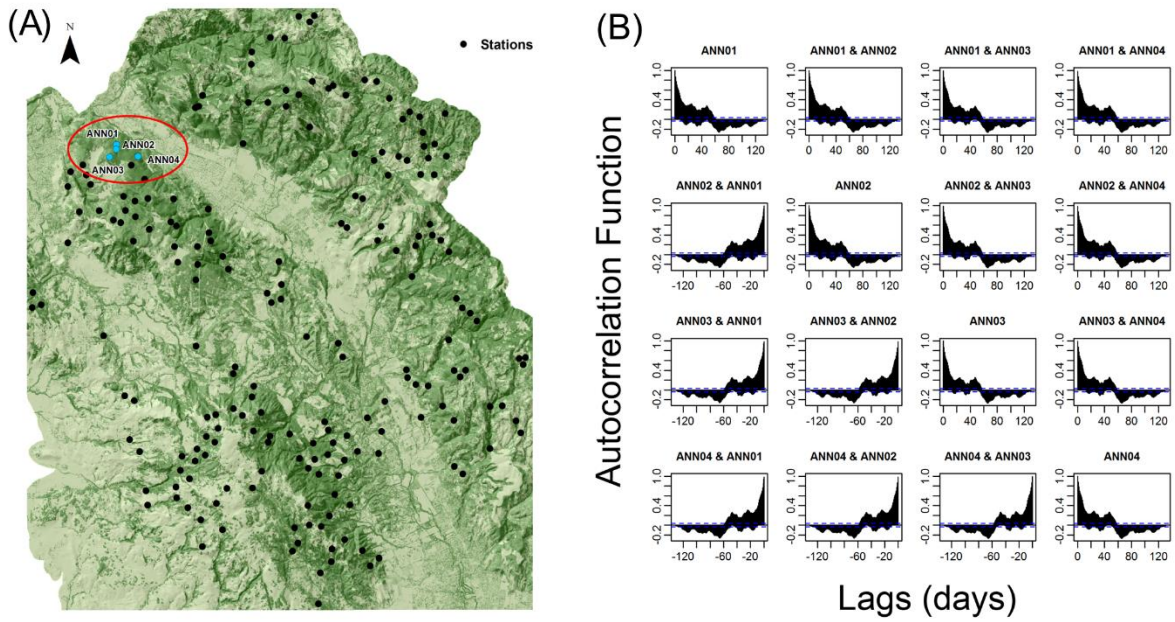
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726 **Figure 5 Temporal cross-correlation between four closely located stations within the study**
 727 **area. (A) Selected stations: ANN01, ANN02, ANN03, ANN04. (B) Cross-correlation plot.**

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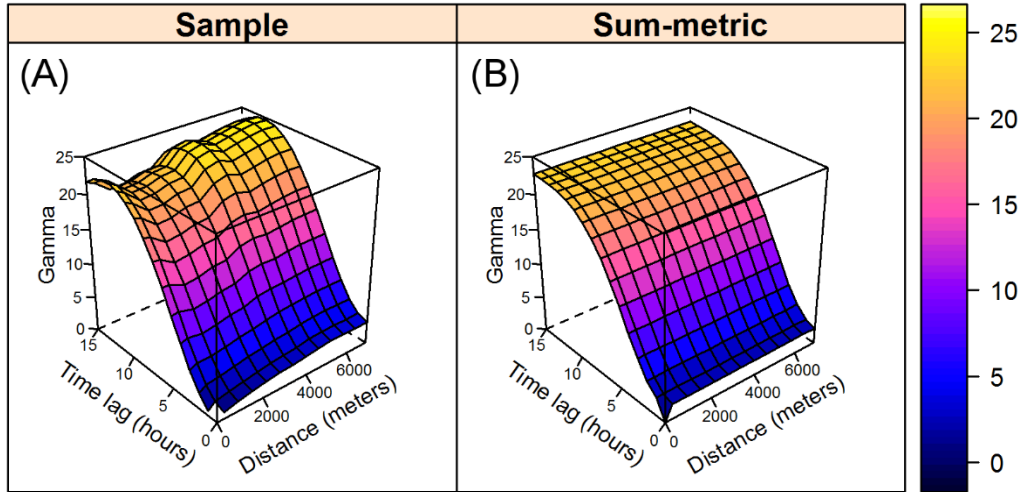
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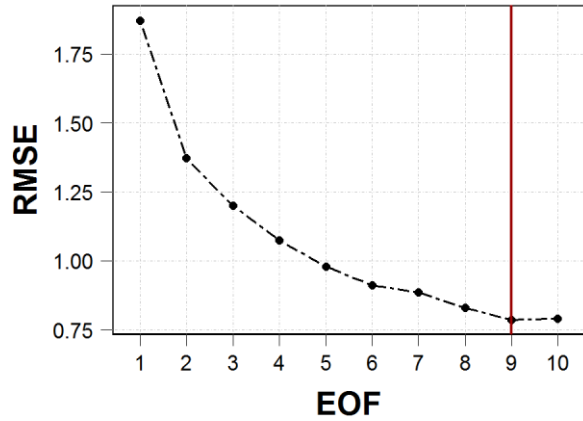
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Figure 6 Sample (left) space-time variogram of residuals from loess smoothing of hourly temperature and fitted (right) sum-metric model. The variogram surface is presented in 3-D. Lighter areas correspond to higher values. Available in colors online.



762

763 **Figure 7 Root-mean-square error calculated for hourly temperature by the iterative**
764 **estimation routine for an increasing number of EOF. The optimal number of EOF (n = 9) is**
765 **chosen based on the convergence criteria set up in the algorithm. Available in colors online.**

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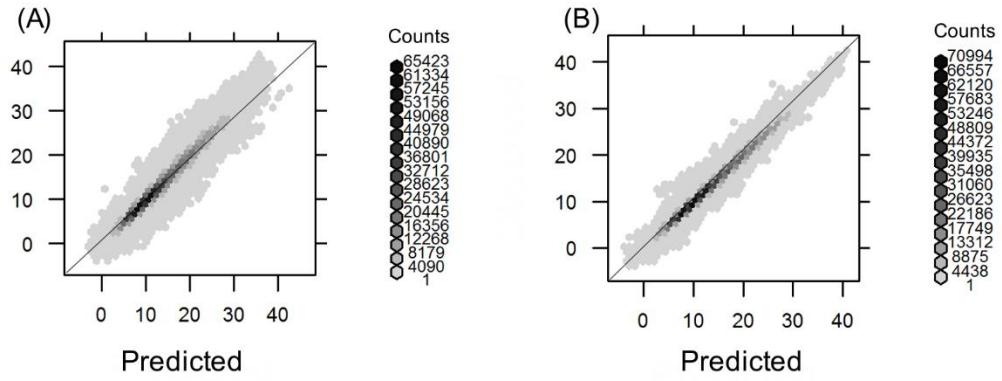
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785 **Figure 8 General relationship between observed and predicted hourly temperature. (A)**

786 **Space-time kriging. (B) Empirical orthogonal functions. Cells along the diagonal are in a**

787 **1:1 relationship. Hexagonal bins are used to group points.**

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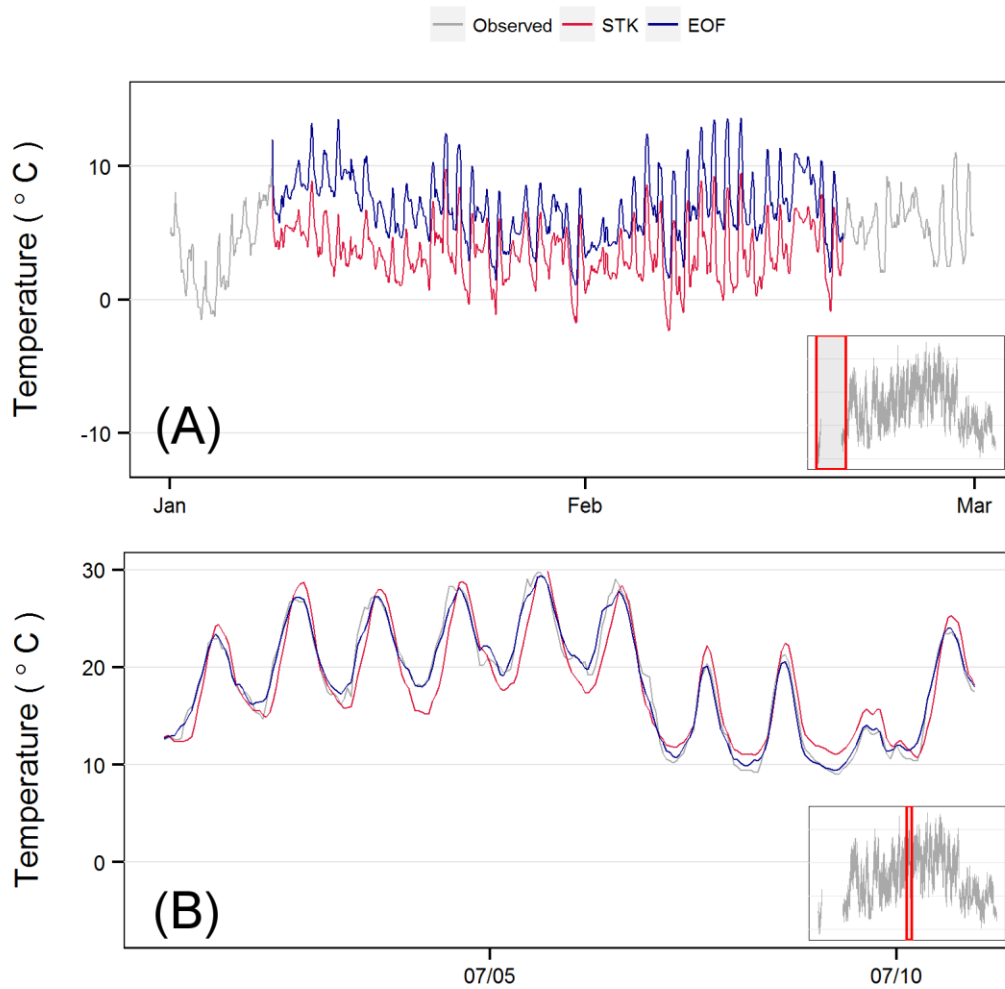
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797 **Figure 9 Hourly temperature (gray line) with overlaid predicted hourly temperature by**

798 **space-time kriging (STK, red line) and empirical orthogonal functions (EOF, blue line) for**

799 **station LARS01. (A) Predictions over a missing section of the dataset. (B) Predictions over**

800 **a complete section of the dataset. Available in colors online.**

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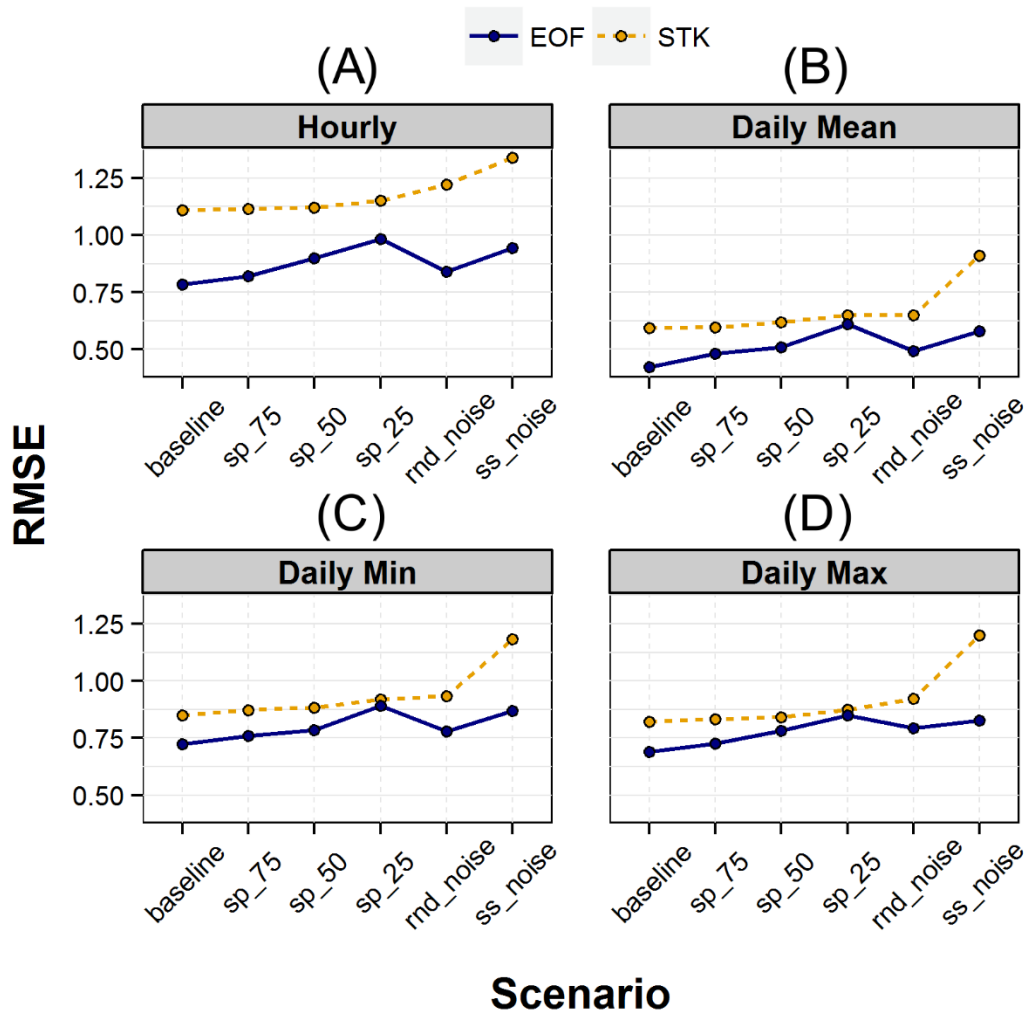
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808 **Figure 10** Root-mean-square error (RMSE) for space-time kriging (STK, golden dashed
 809 **line)** and empirical orthogonal functions (EOF, blue solid line) with different scenarios of
 810 **missing data** (see section 2.4). (A) Hourly temperature (B) Daily mean temperature. (C)
 811 **Daily minimum temperature.** (D) Daily maximum temperature. Available in colors online.

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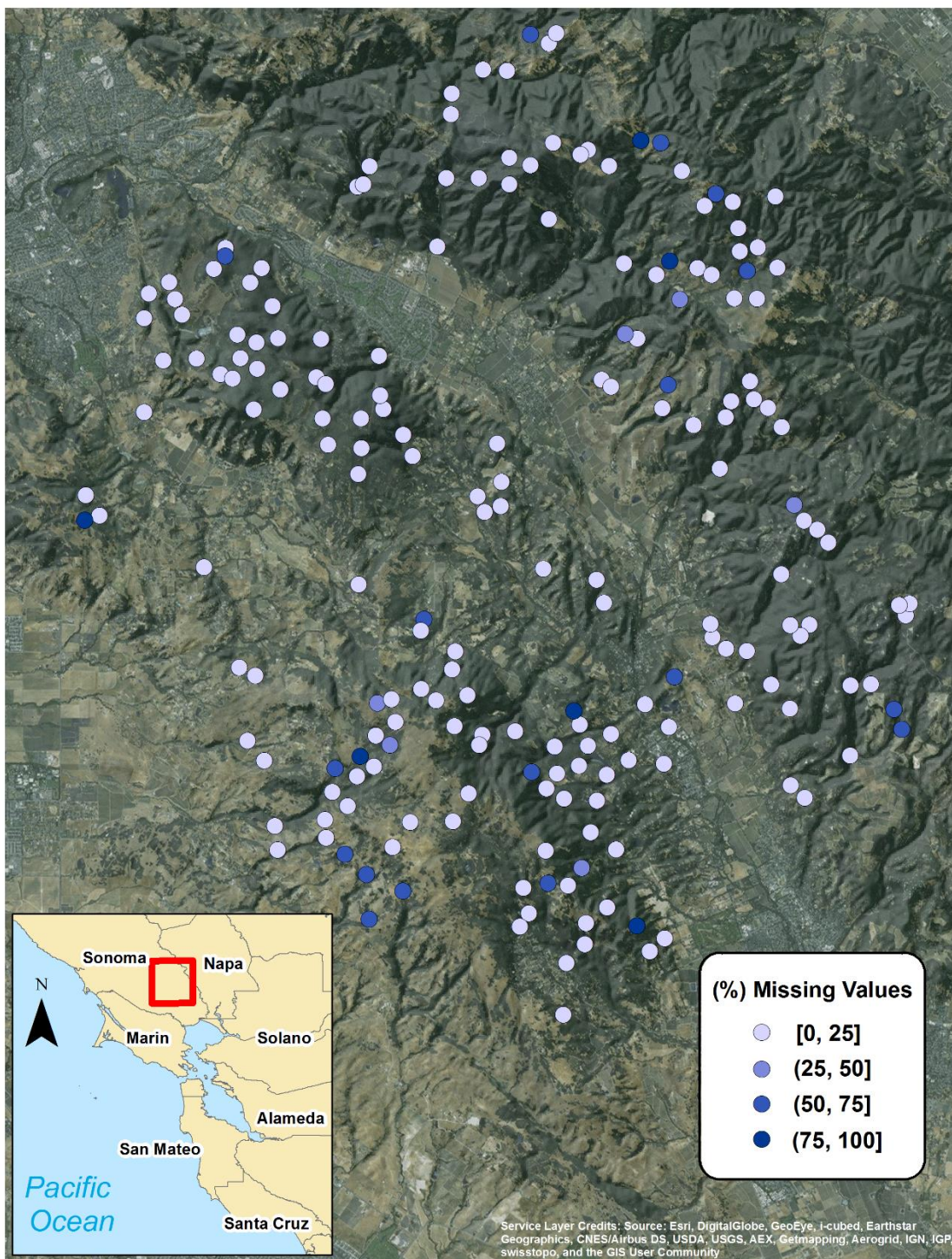
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817 **Table 1 Parameters of the fitted sum-metric variogram model for hourly temperature loess**
 818 **residuals. The model used for each component (see eq.(1)) is also specified.**

	Model	Nugget (semivariance)	Partial Sill (semivariance)	Range	Anisotropy Ratio
Space	Exponential	0	7.21	243.28 km	
Time	Gaussian	0	20.74	6.28 hours	
Joint	Spherical	2.09	7.15	243.47 km	2.96 m/hour

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841 **Figure A.1 Percentages of missing values in the observed understory temperature at each**
842 **microclimate station for the year 2004.**

843 **Appendix B. Empirical Orthogonal Function Estimation Algorithm**

844

845 The following pseudo-code algorithm is illustrated to match the R code we implemented (github
846 link). The structure has been re-adapted from the study by Beckers and Rixen (2003) and the
847 appendix presented in Henn et al. (2013).

848 $\mathbf{X} = m \times n$ ($m = \text{hours}$, $n = \text{stations}$)

849

850 1. Calculate $\mathbf{X_mean}$ (overall dataset mean) and $\mathbf{X_sd}$ (overall dataset standard deviation)

851 2. $\mathbf{X}_0 = \mathbf{X} - \mathbf{X_mean} / \mathbf{X_sd}$ (standardize variable)

852 3. \mathbf{X}_0 [sub] = \mathbf{X}_0_val . Subset portion of data from \mathbf{X}_0 for validation. Replaced with missing
853 values in \mathbf{X}_0 .

854 4. \mathbf{X}_0 [sub] = missing. Values set aside for validation are replaced with missing values in \mathbf{X}_0 .

855 5. \mathbf{X}_0 [missing] = 0; replace all missing values with unbiased guess.

856 6. *Outer FOR LOOP:*

857 FOR N_e (number of EOF) = $\min(n, 30)$; Minimum between number of stations n and 30.

858 $\mathbf{X}_1 = \mathbf{X}_0$; Make a copy of \mathbf{X}_0 . \mathbf{X}_1 will be iteratively improved within the inner loop.

859 7. *Inner FOR LOOP:*

860 FOR k (*iteration*) = 2 to N_{it} (max number of iterations)

861 8. $[\mathbf{U}, \mathbf{D}, \mathbf{V}] = \text{SVD}(\mathbf{X}_1)$; Singular value decomposition (SVD).

862 $\mathbf{U}_t = \mathbf{U}[:, 1:N_e]$; Columns are left singular vectors of \mathbf{X}_1 . Truncate
863 components using first N_e EOFs.

864 $\mathbf{D}_t = \mathbf{D}[1:N_e, 1:N_e]$; Diagonal matrix with singular values. Truncate
865 components using first N_e EOFs.

866 $\mathbf{V}_t = \mathbf{V}[:, 1:N_e]$; Columns are right singular vectors of \mathbf{X}_1 . Truncate
867 components using first N_e EOFs.

868
869 9. $\mathbf{X}_a = \mathbf{U}_t \mathbf{D}_t \mathbf{V}_t^T$; \mathbf{X}_a is the reconstructed matrix.

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871 10. \mathbf{X}_a [!missing] = \mathbf{X}_0 [!missing]; Restore original data in the estimated
872 matrix except where missing in \mathbf{X}_0 .

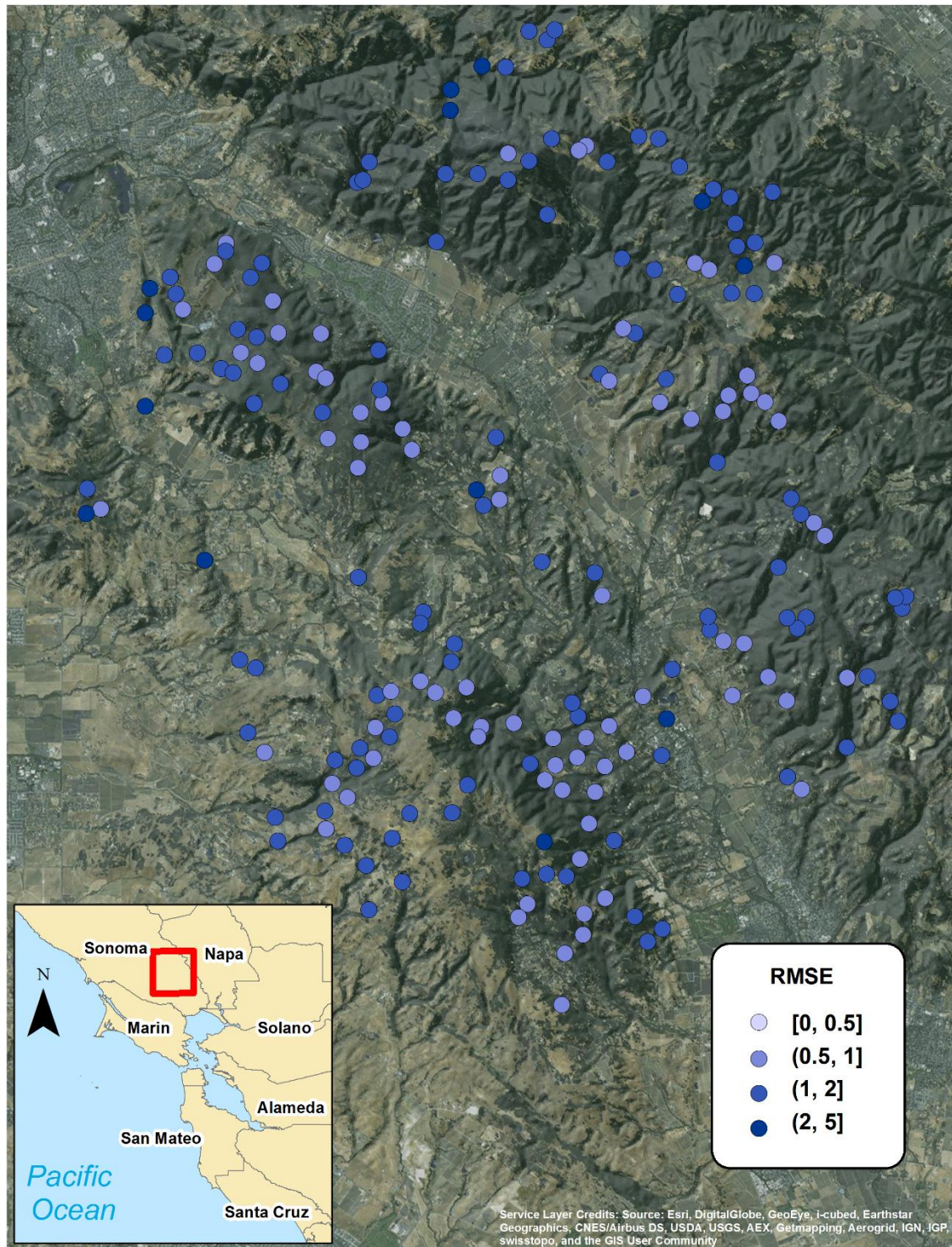
873 11. $dx = \text{sum}[(\mathbf{X}_a - \mathbf{X}_1)^2]$; Calculate deviance of estimated matrix
874 from \mathbf{X}_1 .

875 12. $mx = \text{sum}[(\mathbf{X}_a)^2]$; Calculate deviance of estimated matrix.

```

876 13.          IF dx/mx < tol BREAK (go to outer loop); Test for convergence.
877
878          ELSE  $\mathbf{X}_1 = \mathbf{X}_a$ ; Make a copy of  $\mathbf{X}_a$  and NEXT ( $k = k + 1$ )
879
880 14.           $RMSE[Ne] = \sqrt{(X_a[sub] - X_{0_{val}})^2}$  ; Calculate RMSE using  $Ne$  EOFs.
881
882          IF  $Ne > 1$  & ( $RMSE[Ne - 1] - RMSE[Ne]$ ) < 0.01 BREAK (exit outer
883                                     loop)
884
885          ELSE NEXT ( $Ne = Ne + 1$ ); If the decrease in RMSE is almost zero, exit
886                                     the outer look. Otherwise increase number of
887                                     EOFs by one and restart.
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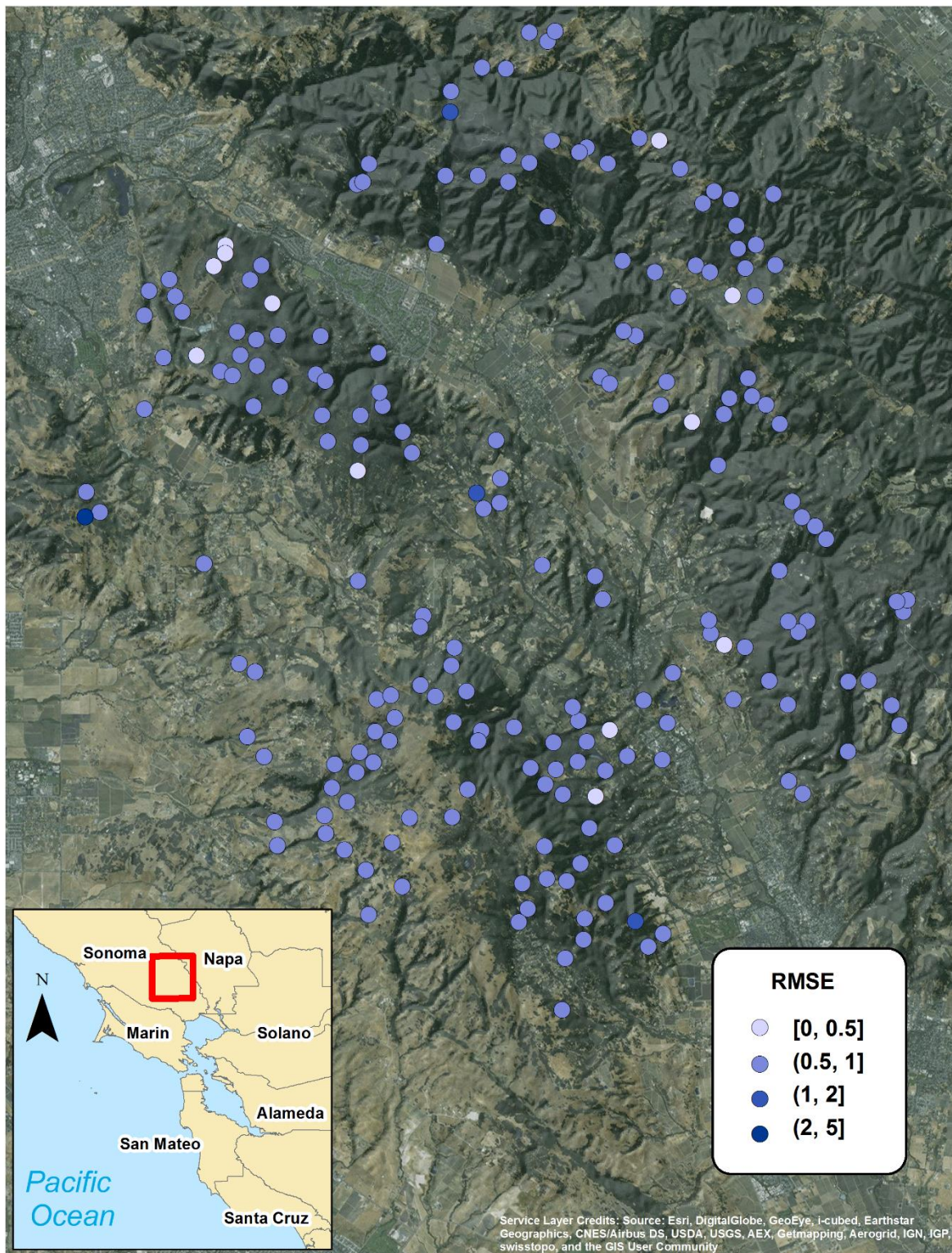



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915 **Figure C.1 RMSE of the predicted hourly temperature at each microclimate station for the**

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year 2004 using STK.



917

918 **Figure C.2 RMSE of the predicted hourly temperature at each microclimate station for the**

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year 2004 using EOF.

920 **Table D.1 Root-mean-square error (RMSE) for space-time kriging (STK) and empirical**
 921 **orthogonal functions (EOF) with different scenarios of missing data at different temporal**
 922 **aggregations.**

		HOURLY					
		baseline	sp_75	sp_50	sp_25	rnd_noise	ss_noise
EOF		0.78	0.82	0.9	0.98	0.84	0.94
STK		1.11	1.11	1.12	1.15	1.22	1.34
		DAILY MEAN					
EOF		0.42	0.48	0.51	0.61	0.49	0.58
STK		0.59	0.59	0.62	0.65	0.65	0.91
		DAILY MINIMUM					
EOF		0.72	0.76	0.78	0.89	0.78	0.87
STK		0.85	0.87	0.88	0.92	0.93	1.18
		DAILY MAXIMUM					
EOF		0.69	0.72	0.78	0.85	0.79	0.83
STK		0.82	0.83	0.84	0.87	0.92	1.20

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925 **Table D.2 Mean Absolute Error (MAE) for space-time kriging (STK) and empirical**
 926 **orthogonal functions (EOF) with different scenarios of missing data at different temporal**
 927 **aggregations.**

		HOURLY					
		baseline	sp_75	sp_50	sp_25	rnd_noise	ss_noise
EOF		0.56	0.58	0.61	0.68	0.62	0.64
STK		0.93	0.92	0.93	0.96	0.97	1.02
		DAILY MEAN					
EOF		0.37	0.41	0.45	0.51	0.44	0.52
STK		0.48	0.49	0.49	0.50	0.53	0.60
		DAILY MINIMUM					
EOF		0.52	0.55	0.59	0.66	0.58	0.63
STK		0.75	0.77	0.77	0.79	0.81	0.95
		DAILY MAXIMUM					
EOF		0.48	0.52	0.58	0.64	0.61	0.65
STK		0.73	0.74	0.77	0.77	0.80	0.91

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930 **Table D.3 Correlation (COR) for space-time kriging (STK) and empirical orthogonal**
 931 **functions (EOF) with different scenarios of missing data at different temporal**
 932 **aggregations.**

		HOURLY					
		baseline	sp_75	sp_50	sp_25	rnd_noise	ss_noise
EOF		0.95	0.92	0.89	0.87	0.93	0.88
STK		0.94	0.93	0.91	0.89	0.90	0.87
		DAILY MEAN					
EOF		0.97	0.94	0.92	0.91	0.92	0.90
STK		0.96	0.96	0.94	0.93	0.92	0.89
		DAILY MINIMUM					
EOF		0.93	0.91	0.89	0.85	0.91	0.88
STK		0.89	0.89	0.88	0.86	0.89	0.84
		DAILY MAXIMUM					
EOF		0.94	0.92	0.91	0.88	0.92	0.89
STK		0.92	0.92	0.89	0.89	0.88	0.85

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934 **Table D.4 Mean-square-error skill Score (SS_{MSE}) for space-time kriging (STK) and**
 935 **empirical orthogonal functions (EOF) with different scenarios of missing data at different**
 936 **temporal aggregations.**

		HOURLY					
		baseline	sp_75	sp_50	sp_25	rnd_noise	ss_noise
EOF		0.98	0.97	0.95	0.92	0.93	0.90
STK		0.93	0.93	0.90	0.90	0.91	0.86
		DAILY MEAN					
EOF		0.96	0.95	0.94	0.92	0.92	0.91
STK		0.96	0.95	0.95	0.93	0.93	0.87
		DAILY MINIMUM					
EOF		0.94	0.94	0.92	0.89	0.90	0.88
STK		0.91	0.91	0.91	0.90	0.89	0.85
		DAILY MAXIMUM					
EOF		0.96	0.95	0.92	0.88	0.92	0.89
STK		0.94	0.92	0.91	0.91	0.89	0.87

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